Financial derivatives are financial instruments which enable investor or a debtor to optimize his/her asset/debt portfolios according to individual needs and acceptable scale of risk. Their importance in financial markets rose enormously n past ten years as well as did their traded volumes. Interest rate derivatives form a large sub-group of financial derivatives, their valuation is a large self-contained chapter within financial mathematics thanks to the unique characteristics of yield- and discount-curve dynamics. In the first part of my thesis I derive the fundamental pricing principles stemming from no-arbitrage pricing theory and introduce the most common approaches in yield curve modeling. In the second part I discuss issues of calibration in a "LIBOR Market Model" with one to three risk factors. These models are used to price swaptions with Monte Carlo simulation within the no-arbitrage framework introduced in the first part. The result of the thesis is that one factor model performs the best in pricing swaptions.