This work systematically studies the concept of compactness in classical propositional logic as well as various concepts of compactness and their relation to different notions of completeness in the framework of the general theory of consequence relations. It also considers the compactness in various basic non-classical logics – fuzzy and modal propositional fuzzy logics.