In the thesis we introduce arithmetic geometric mean sequences, firstly over real numbers and then over finite fields $\mathbb{F}_{q}$ such that $q \equiv 3(\bmod 4)$. We connect the sequences with graphs and prove some properties over general finite fields for these graphs. We also extend arithmetic geometric mean sequences over $\mathbb{F}_{q}$ such that $q \equiv 5(\bmod 8)$ and we show a connection between elliptic curves and arithmetic geometric mean sequences over $\mathbb{F}_{q}$ such that $q \equiv 3(\bmod 4)$.

