The work is focused on the structure of triangulations of combinatorial surfaces. By analyzing several local reduction moves and one global move, several known results are proven in a new way. This includes the fundamental inequality for the Euler characteristic, Fáry's theorem, and the existence of two local moves that can be used to obtain all Eulerian combinatorial spheres from an octahedron, more precisely every triangulation of sphere in which each vertex has even degree.