

Title: Distance Magic Labelings

Author: Hayden Pfeiffer

Department: Dept. of Theoretical Computer Science and Mathematical Logic

Supervisor: doc. Mgr. Petr Gregor, Ph.D., KTIML, MFF UK

Abstract: A distance magic labeling of a graph  $G$  is a bijection  $f : V(G) \rightarrow \{1, 2, \dots, |V(G)|\}$  such that the sum of labels on the neighbourhood of each vertex is constant. A framework based on linear algebra has been developed using the notion of neighbour balance to determine whether there exists a distance magic labeling for a hypercube with dimension  $n$ . In this thesis, we extend this framework to all Cayley graphs on  $\mathbb{Z}_2^n$ . We use this framework to reprove some known results from recent literature. We also use this framework to introduce the notion of *component-wise* distance magic labelings on Cayley graphs of  $\mathbb{Z}_2^n$ .

Keywords: distance magic labeling, Cayley graph, hypercube, neighbour balance