The flow in porous media can be described by the Richards equation. However, porous media often exhibit a variety of heterogeneities, thus treating a porous medium as homogeneous does not often fit the reality well. Therefore, we describe the flow in the porous medium using the Richards equation with the dual-permeability model, which assumes that the porous medium can be separated into two different media. This thesis is concerned with the numerical solution of the Richards equation with the dualpermeability model. We present the derivation of the dual-permeability model, and for the numerical solution, we use the space-time discontinuous Galerkin method. This produces a system of nonlinear algebraic equations that need to be linearized. We perform a 1D experiment to verify the method and, finally, we present a 2D single-ring experiment to demonstrate the method.