The main result of the work is a complete discussion of the solutions to stochastic differential equations on the half-line $(0, \infty)$ with polynomial coefficients in terms of their lifetimes. To achieve this, Feller's test for non-explosion is utilized. The theorem is proven in detail, as existing proofs are too concise.