

The thesis consists of three articles. The common theme of the first two articles is the possibility of iterating weak\* derived sets in dual Banach spaces. In the first article we prove that in the dual of any non-reflexive Banach space we can always find a convex set of order  $n$  for any  $n \in \mathbb{N}$ , and a convex set of order  $\omega + 1$ . This result extends Ostrovskii's characterization of reflexive spaces as those spaces for which weak\* derived sets coincide with weak\* closures for convex sets. In the second article we prove an iterated version of another result of Ostrovskii, that a dual to a Banach space  $X$  contains a subspace whose weak\* derived set is proper and norm dense, if and only if  $X$  is non-quasi-reflexive and contains an infinite-dimensional subspace with separable dual. In the third article we study quantitative results concerning  $\xi$ -Banach-Saks sets and weak  $\xi$ -Banach-Saks sets. We provide quantitative analogues to characterizations of weak  $\xi$ -Banach-Saks sets using  $\ell_1^{\xi+1}$  spreading models and a quantitative version of the relation of  $\xi$ -Banach-Saks sets, weak  $\xi$ -Banach-Saks sets, norm compactness and weak compactness. We use these results to define a new measure of weak non-compactness and finally give some relevant examples.